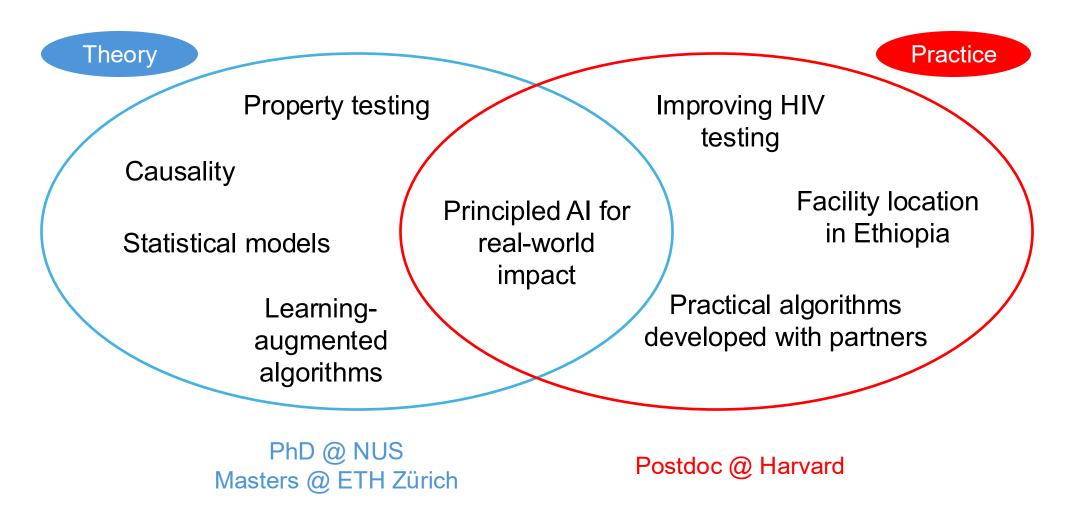
# Principled AI for Real-world Impact: Structured Decision-Making under Uncertainty

**Davin Choo** 

Postdoctoral Fellow @ Harvard SEAS

## Research vision: Principled AI for real-world impact



## Research vision: Principled AI for real-world impact



# For this talk, I will share about two projects that I (co-)led at Harvard



PhD @ NUS
Masters @ ETH Zürich

Postdoc @ Harvard

## Roadmap for this talk

Project 1: Adaptive disease testing on graphs [1]

Project 2: Health facility planning in Ethiopia [2]

Lessons learnt and personal takeaways

[1] **Davin Choo**, Yuqi Pan, Tonghan Wang, Milind Tambe, Alastair van Heerden, and Cheryl Johnson. Adaptive Frontier Exploration on Graphs with Applications to Network-Based Disease Testing. Under submission, 2025.

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## **Project 1**

Adaptive disease testing on graphs [1]



Yuqi
Pan
Harvard University



Tonghan
Wang
Harvard University



Milind
Tambe
Harvard University



Alastair
van Heerden
University of Witwatersrand
Wits Health Consortium

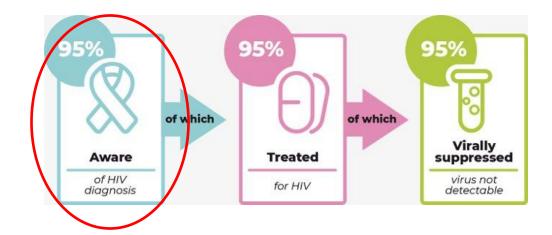


Cheryl
Johnson
World Health
Organization

## Targeting the first 95% in the 95-95-95 initiative

## Global initiative by UNAIDS to control the HIV epidemic

- Undetectable = Untransmittable (U = U)
- UN Sustainable Development Goal 3.3



#### **Motivation**

- The faster we detect positive cases, the faster we can start treatment cascade
- Once individuals learn about their status, they will also typically undergo behavioral changes which help limit spread

#### Challenges

- In 2024, WHO estimates that 1 in 7 HIV positive individuals do not know they are infected
- Resource limitations due to funding cuts

## Current testing approaches and challenges

## Variety of differentiated testing services address different settings and populations

- Demand creation
- Self-testing
- Facility/community/network-based testing



## Reduced effectiveness / Diminishing returns as we approach 95% in the testing goal

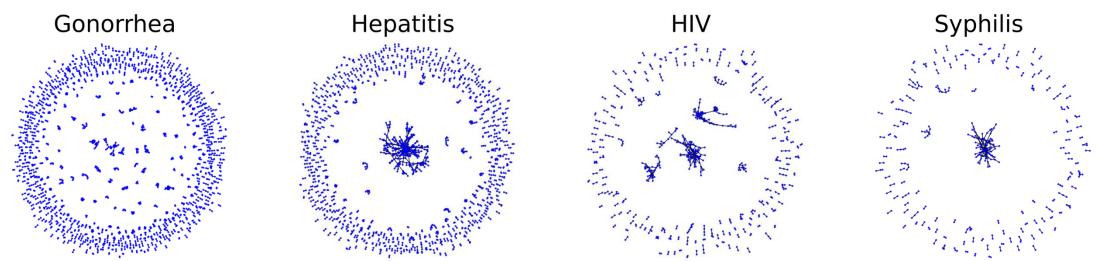
- Currently, questionnaires are used to collect data from individuals then derive a "risk score"
  - Each person is given associated with an anonymous ID
  - Also collect individual information (e.g., age, occupation, living region, personal beliefs, alcohol/drug tendencies, etc.), as well as the IDs of sexual and drug-injecting partners
- Current testing prioritization does not effectively exploit disease transmission network
- New approaches and ideas are needed for increasing reach and testing effectiveness

## Re-imagining a new testing approach

#### **Objective**

- Maximize efficiency of testing resources in detecting HIV+ cases as quickly as possible
  - Resource can be # test kits, or where to focus efforts of human workers in recruiting people for testing

- Sexually transmitted diseases do not spread like flu
  - The transmission graph g is sparse and tree-like
  - Note: We only ever observe a subset of the true graph

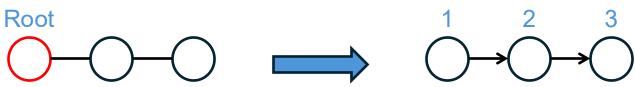


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  - This is because it is more informative than randomly picking individuals to test next
  - This maps to a kind of "frontier exploration" constraint on the graph
  - First tested person (the root) of each component is chosen via some domain policy consideration



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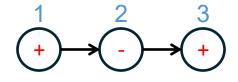
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  - This maps to a kind of "frontier exploration" constraint on the graph
  - First tested person (the root) of each component is chosen via some domain policy consideration
- There is some underlying transmission probability  $\mathcal P$  that is Markov with respect to  $\mathcal G$ 
  - Every individual has an unobserved discrete label of + or -, that is revealed upon testing
  - Markov:  $\mathcal{P}(\text{person} = + | \text{revealed status}) = \mathcal{P}(\text{person} = + | \text{revealed statuses of neighbors})$

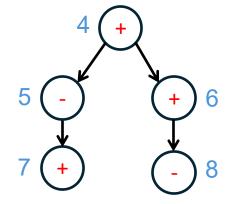
## Designing a reward metric for optimization

#### Illustrative example

- Suppose we know the underlying labels (disease status)
- How good is this sequence of testing?
  - Early detection → early intervention; Also, we may have sudden budget cuts

Testing budget	1	2	3	4	5	6	7	8
# positive detected	1	1	2	3	3	4	5	5





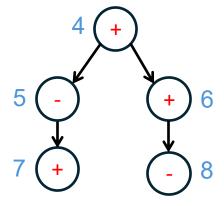
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	_	3
( + )—	→( - )—	→( + )

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#### **Reward metric**

- Use discount factor  $\beta \in (0, 1)$  to favor early discovery of positive cases
  - This sequence :  $\beta^0 * 1 + \beta^1 * 0 + \beta^2 * 1 + \beta^3 * 1 + \beta^4 * 0 + \beta^5 * 1 + \beta^6 * 1 + \beta^7 * 0$

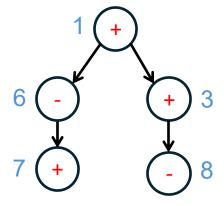
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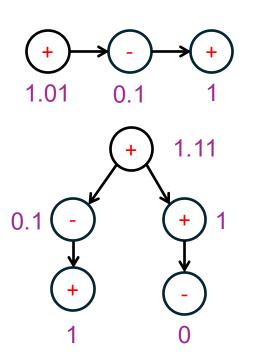
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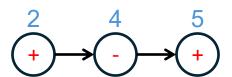


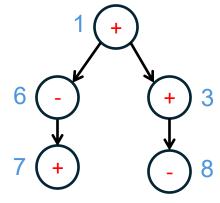
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  - A better sequence:  $\beta^0 * 1 + \beta^1 * 1 + \beta^2 * 1 + \beta^3 * 0 + \beta^4 * 1 + \beta^5 * 0 + \beta^6 * 1 + \beta^7 * 0$
- Finding a sequence to optimize this reward metric helps detect positive cases faster, for any fixed amount of testing budget

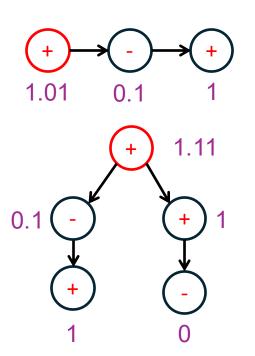
- Compute a score\* for each node, then greedily select from the nodes in the frontier
- Known to produce an optimal sequence on our reward metric when the input graph is a forest

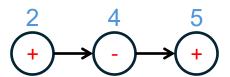


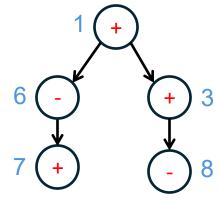




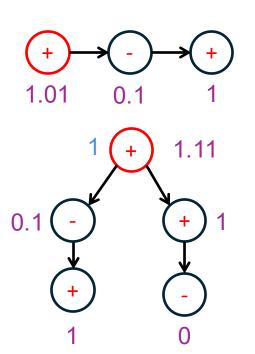
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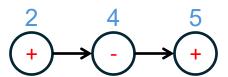


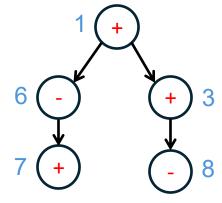




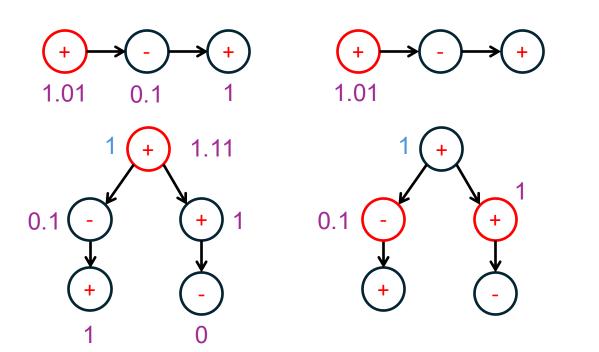
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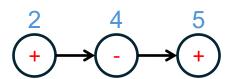


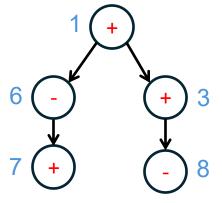




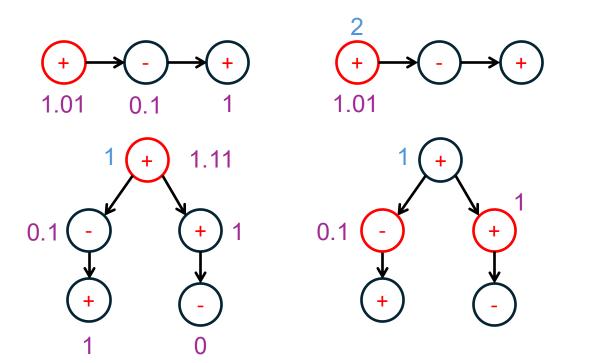
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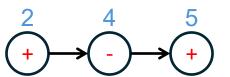


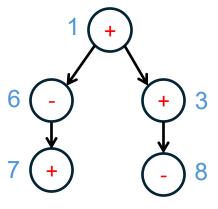




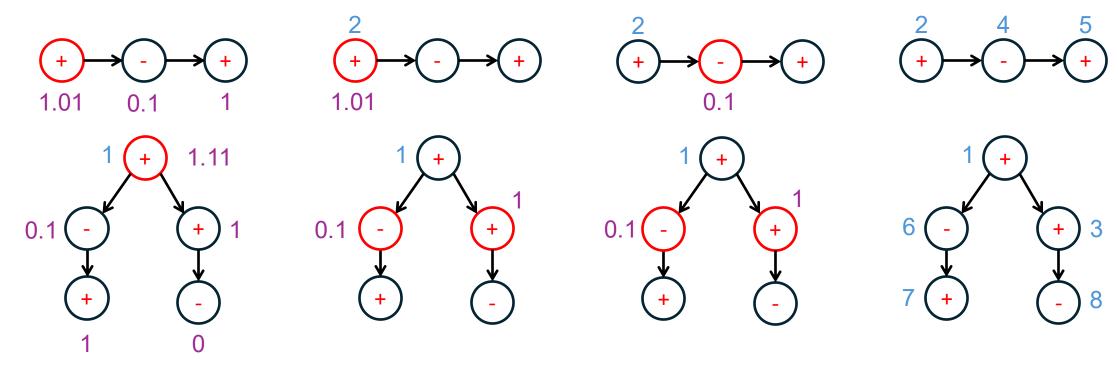
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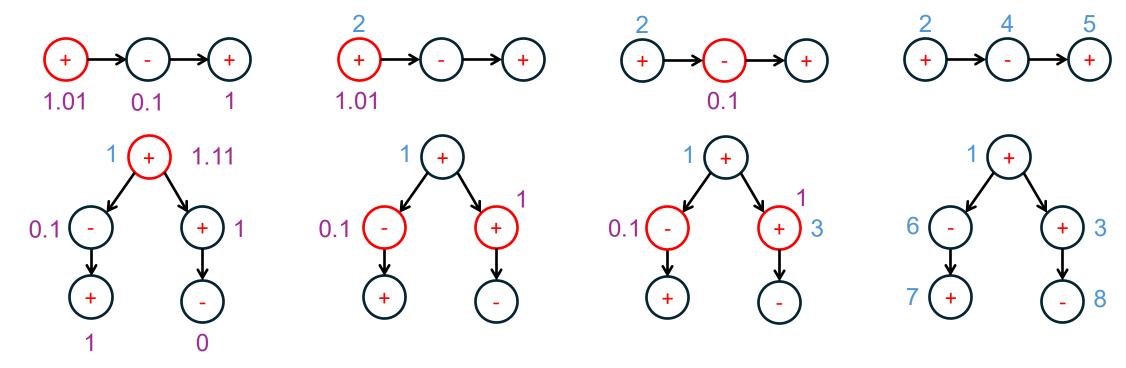


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<sup>19</sup> 

- Compute a score\* for each node, then greedily select from the nodes in the frontier
- Known to produce an optimal sequence on our reward metric when the input graph is a forest



<sup>20</sup> 

#### Using the idea of Gittins indices for our example

- Compute a score\* for each node, then greedily select from the nodes in the frontier
- Known to produce an optimal sequence on our reward metric when the input graph is a forest

#### This approach generalizes to rooted forests and probabilistic labels

- Statuses can be a function of the revealed parent's status, based on a known distribution  $\mathcal{P}$
- Now, we pre-compute a score for node X based on every possible parent status, then use the score that corresponds to revealed parent status when ranking node X in the frontier

To define the Gittins index, let us first define two recursive functions  $\phi$  and  $\Phi$ , as per [KO03]. For any non-root node  $X \in \mathbf{X}$ , label  $b \in \Sigma$ , and value  $0 \le m \le \frac{\bar{r}}{1-\beta}$ ,

## Using the idea of (

$$\phi_{X,b}(m) = \max \left\{ m, \sum_{v \in \Sigma} \mathcal{P}(X = v \mid \text{Pa}(X) = b) \cdot \left[ r(X, v) + \beta \cdot \Phi_{\text{Ch}(X), v}(m) \right] \right\}$$
(1)

• Compute a scc efforts:  $\text{Enown to prod} \text{ If } X \text{ is the root, we define } \phi_{X,\emptyset}(m) = \max \left\{ m, \sum_{v \in \Sigma} \mathcal{P}(X = v) \cdot \left[ r(X,v) + \beta \cdot \Phi_{\mathrm{Ch}(X),v}(m) \right] \right\} . \text{ out graph is a forest prodest}$ For any subset of nodes  $S \in X$ , label  $b \in \Sigma$ , and value  $0 \le m \le \frac{\bar{r}}{1-\beta}$ ,

$$\Phi_{\mathbf{S},b}(m) = egin{cases} rac{ar{r}}{1-eta} - \int_m^{rac{ar{r}}{1-eta}} \prod_{Y \in \mathbf{S}} rac{\partial \phi_{Y,b}(k)}{\partial k} \ dk & ext{if } \mathbf{S} 
eq \emptyset \\ m & ext{if } \mathbf{S} = \emptyset \end{cases}$$

(2) wn distribution  ${\cal P}$ 

Gittins index for node X when parent's realization is b a score  $g(X,b) = \min \left\{ m \in \left[0,\frac{\bar{r}}{1-\beta}\right] : \phi_{X,b}(m) \ge m \right\}$  This "min  $\ge$ " captures the intuition of "fair value"

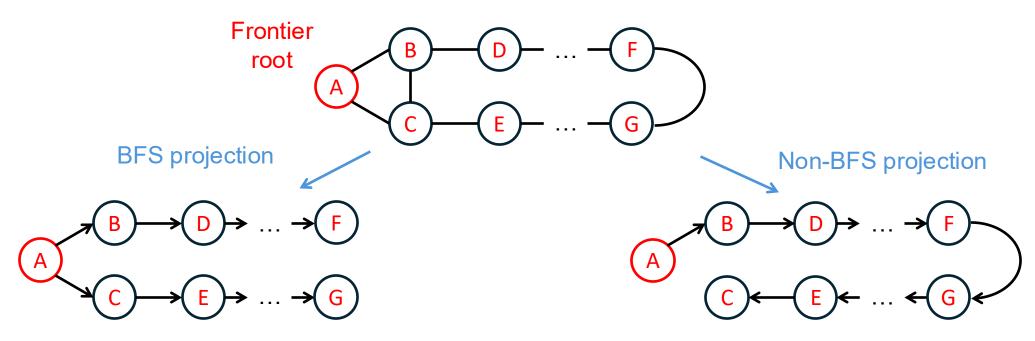
## We show that our adaptive testing problem can be reduced to "branching bandits"

- Optimality of Gittins indices for rooted forests proven in [KO03]
- We provide the first efficient polynomial time dynamic programming (DP) method (with working) Python code) in the 20 years since [KO03] for computing φ and Φ for *discrete labels* 
  - Prove and exploit piecewise linearity of  $\phi$  and  $\Phi$ , enabling efficient representation of  $\phi$  and  $\Phi$  in the DP
  - Number of pieces scale with the number of nodes and number of labels

# In practice, use BFS to project non-trees into trees before applying Gittins computation

## Transmission graphs g may not be forests in general

- Run breadth-first search (BFS) on  $\mathcal{G}$  from the frontier roots in each component
- This minimizes height to root, reducing artificial frontier constraint due to projection



C can still be reached by A after 1 step

This projection requires multiple steps between A and C

## Some experimental results

## Assume that G and P are provided as input

- g is subgraph of disease-specific interaction graph involving ~300 nodes
- $\mathcal{P}$  is an Ising model, i.e., Markov random field (MRF) with unary and pairwise potentials  $\theta$
- Train  $\mathcal{P}$  from disease-specific past data, i.e., fit  $\theta$  via pseudo-likelihood
- Measure *expected* performance, with respect to  $\mathcal{P}$

#### **Baselines**

- Random: Randomly select next frontier node to test
- Greedy: Select frontier node with highest posterior probability of being positive
- DQN: Deep Q-network using message-passing GNN with edge-conditioned weights

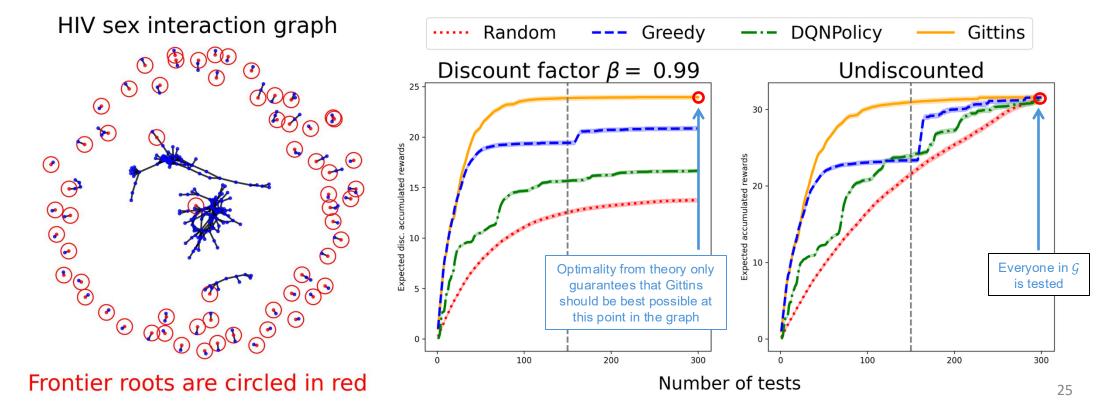
#### **Additional remarks**

- MRF computations are reasonable on low treewidth graphs via Junction tree algorithm
- For small graphs (~10 nodes) where we can brute-force compute the optimal policy, we verified that Gittins literally traces the optimal curve, unsurprisingly

## Empirical evaluation on HIV interaction graph

With only budget to test half the population, Gittins detects almost all positive cases in expectation while the other methods still miss about 25% of the positive cases

• Similar trend for other disease graphs; Gittins always "the best" (see backup slides)



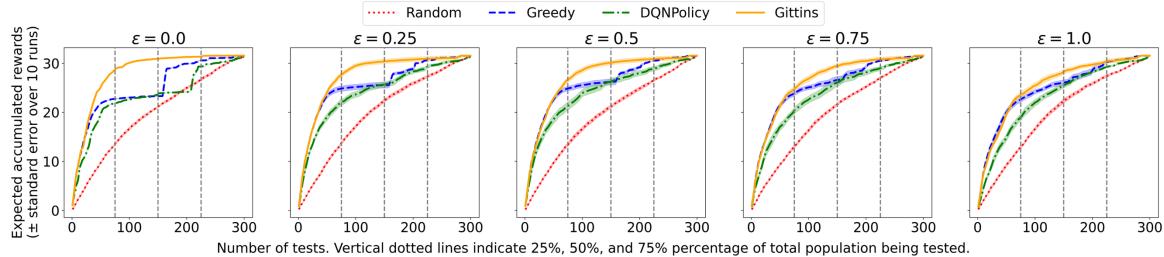
# Trend remains empirically robust even when policies only have access to noisy estimate Q of P

## Generate noisy distribution Q by adding noise to $\mathcal P$

- $\mathcal{P}$  is an Ising model, i.e., Markov random field with unary and pairwise potentials  $\theta$
- Q is defined by adding noise to θ
- For different  $\epsilon$ , add  $\epsilon$  \* u \*  $|\theta_i|$  to i-th coordinate of  $\theta$ , where u ~ Uniform(-1, 1)

## Empirical advantage of Gittins decreases as noise increases

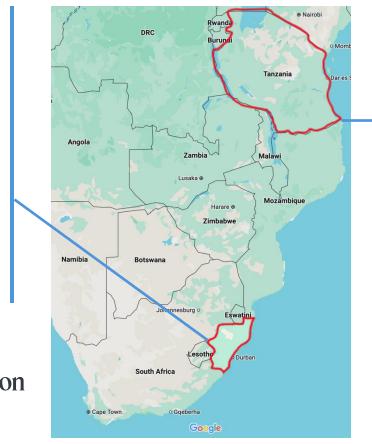
Below: Undiscounted accumulated reward plot for the same HIV interaction graph



# Next steps: Working towards a field trial and a more comprehensive retrospective study

## **Trial-run deployment**

- In collaboration with WHO and the Gates foundation, under the HIV LIFT project
- Deployment area: KwaZulu-Natal, South Africa



## Comprehensive retrospective study

- In collaboration with FHI 360<sup>1</sup>
- Currently drafting concept note and data agreement to get access anonymized Tanzanian program data to perform a more comprehensive retrospective study of our method



World Health Organization

**Gates Foundation** 

27

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## Project 2

# Health facility planning in Ethiopia [2]



Yohai Trabelsi

Harvard University



Fentabil Getnet

National Data Management and Analytics Center for Health, Ethiopian Public Health Institute



Samson Warkaye Lamma

National Data Management and Analytics Center for Health, Ethiopian Public Health Institute



Wondesen Nigatu

Primary Healthcare and Community Engagement Lead Executive Office, Ministry of Health



**Kasahun Sime** 

Primary Healthcare and Community Engagement Lead Executive Office, Ministry of Health



Lisa Matay

Department of Global Health and Population, Harvard T.H. Chan School of Public Health



Stéphane Verguet

Department of Global Health and Population, Harvard T.H. Chan School of Public Health



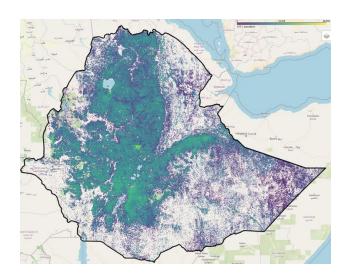
Milind Tambe

Harvard University

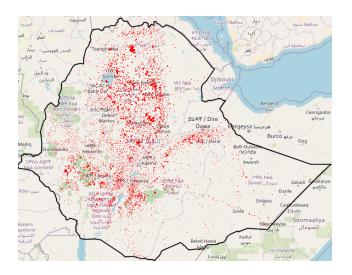
## 72% of the population lack access to "comprehensive health care" within 2 hours of walking

## There is a desire to improve access to "comprehensive health care" in Ethiopia

- 2<sup>nd</sup> most populous country in Africa, with ~130 million people, ~76% live in rural areas
- Walking is most common form of transport in rural areas
- In line with UN Sustainable Development Goal 3.8



Population of Ethiopia in log scale (brighter spots are denser areas)



Areas within 2 hours of walking by existing facility capable of "comprehensive health care"

## Formalizing the facility location problem

#### **Objective**

Maximize access to "comprehensive health care" over 5-year planning horizon

## Available data (that is also used by the Ethiopian officials when planning)

- Population forecasts via WorldPop projections in 1km-by-1km grids
- Point-to-point walking distance estimates [WNVR+20]
- List of existing facilities and estimated yearly regional budget from Ethiopia officials

- Decision making and budget availability mainly at regional level
- Each region has different "fairness" prioritization over districts
- Uncertainty in future budget due to unforeseen budget cuts or donors

## Formalizing the facility location problem

#### **Objective**

Maximize access to "comprehensive health care" over 5-year planning horizon

## Problem modeling: "Some variant of maximum coverage"

- Maximize access → Maximize monotone submodular function
- 5-year horizon with budget uncertainty → Online setting with irrevocable decisions
- Budget and proportionality constraints → Matroid constraints

- Decision making and budget availability mainly at regional level
- Each region has different "fairness" prioritization over districts
- Uncertainty in future budget due to unforeseen budget cuts or donors

## Solving the "maximum coverage" variant

## Maximizing non-decreasing submodular functions is well-studied

- Hard problem, even to approximate
- Greedy (based on marginal gain) is more or less the best we can hope for, in terms of approximation guarantees, when restricting to polynomial time algorithms [NWF78, FNW78]
- Cannot obtain better approximation ratio unless P = NP [Fei98]

## Designing a learning-augmented algorithm to exploit domain expertise

- Currently, given a fixed budget, regional experts will consult/interview citizens, conduct field measurements, etc. and then produce a selection **A** based on their domain knowledge
- Let G be the selection produced by the greedy algorithm that is independent produced
- We can actually produce a unified selection **U** such that
  - The selection U respects the same constraints as the selections A and G
  - f(U) ≥ max { f(A), f(G) }, where f measures the multi-year access to "comprehensive health care"
  - There are instances where the inequality is strict

## Next steps: A tool and a public health study

#### With Harvard T.H. Chan School of Public Health and officials from Ethiopia

- Build an actual tool and perform user studies with Ethiopian regional planners
- Study the usefulness and impact of our proposed method from a public health perspective



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## Lessons learnt and personal takeaways

## 1. A useful problem formulation is a non-trivial contribution

A good problem formulation is half the battle won

"Often, the most important step is making the right notion, defining the right notion. Once you have the right notion, you know, the rest of the theory, theorems, proofs, [and] constructions follow."



Avi Wigderson, 2023 Turing award winner

## 2. Real-world settings often have structures to exploit

• Principally designed methods can beat simple heuristics, even if assumptions are imperfect

## 3. Learning-augmented algorithms are a powerful and practical tool

• Improve processes while respecting domain expertise in the age of AI and getting buy-in

## Special thanks to all my amazing collaborators on my research journey!















































































## Back up slides

## Sample of questionnaire questions

#### Each person is associated with an anonymous ID

#### Individual characteristics

The first thing I would like to do is ask you some general background questions. (race,

education, and living situation)		
A. DEMOGRAPHICS		
1. Record sex as observed:	Male	1
2a. What is your date of birth, mo		
	month day year	_
b. How old are you?y	rears (Check age with date of birth)	
3. Record racial or ethnic backgro	ound:	
	African American, Black Non-Hispanic	2
3	White, Hispanic	5
4. What is the highest grade of so	shool you've completed?	
12	Grade (1-11) High School Diploma  GED Some College College	1
17	Graduate School	
5a. What is your marital status?		
	Married Separated Divorced Widowed Single [Ask 5h]	3

#### Personal beliefs

#### H. AIDS INFORMATION

Thank you for all of your answers about HIV and your health status. Now I'm going to ask you some questions about opinions about HIV/AIDS.

Strongly Kind of Kind of Strongly

#### \* If HIV Positive, skip question(s)

		Agree	Agree	Disagree	Disagree
1.	Injection drug users are at risk for getting AIDS.	1	2	3 4	
2.	Cleaning works with soap and	1	2	3 4	
۷.	water kills the AIDS virus.	1	2	3 4	
3.	Cooking the drugs will kill the HIV virus.	1	2	3 4	
4.	Natural skin condoms are protective against HIV.	1	2	3 4	
5.	People are likely to get AIDS if they bleach their works before sharing them.	1	2	3 4	
6.	The AIDS virus was started by an experiment that went wrong.	1	2	3 4	
7.	If it's meant to be I will get the AIDS virus.	1	2	3 4	
8.	You've got to die of something someday - it might as well be AIDS!	1	2	3	4
9.	AIDS was created to kill blacks and poor folks.	1	2	3	4
10.	Most research projects don't help the community.				

#### Sexual and drug-injecting partners

94 Please tell me the FIRST NAME and the FIRST INITIAL OF THE LAST NAME of all the different people with whom you have had close personal contact, had sex, taken drugs, or shared needles with during the past 6 months (give respondent a specific date [a benchmark] to go back to). Start with current people and work your way back.

ENTER ALL NAMES ONTO THE FIRST, DOUBLE-SIDED MATRIX . AFTER THE NAMES ARE WRITTEN DOWN:

Now I would like to ask you a few questions about these people.

- 95 For each person, please tell me how long you have known them
- 96 Which of these people are related to you, by either blood or marriage?
- 97 Which of these people are neighbors (live within easy walking distance)?
- 98 Which of these people are coworkers (people you work with)?
- 99 How would you describe the people you've named who are neither relations, neighbors, or coworkers?
- 100 How often have you seen each of these people in person in the last 3 months?

Codes for Frequency of Contact:

0 = not at all1 = once or twice

2 = three to six times

3 = at least a couple of times a month

4 = weekly

5 = daily

97 = not asked

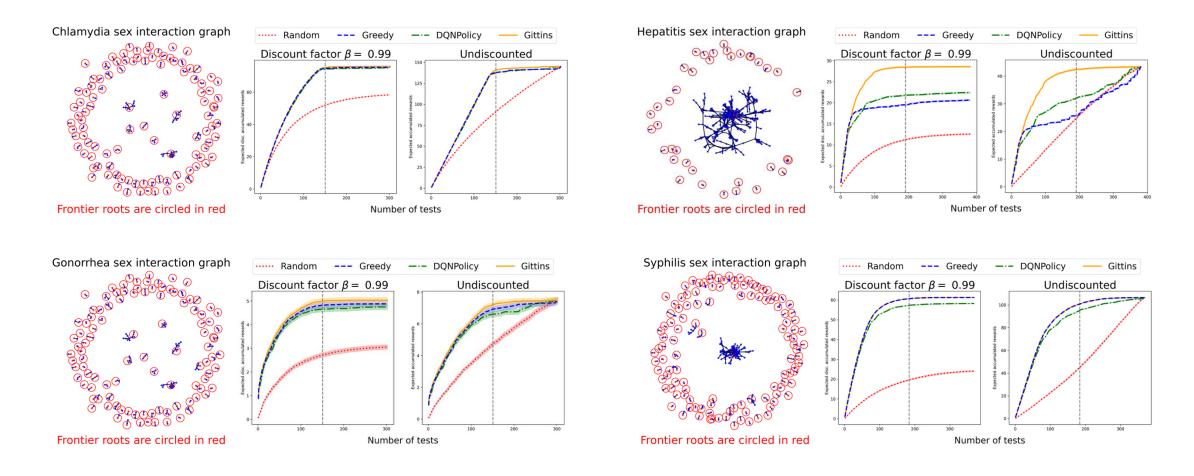
98 = refused

99 = not known

- 101 Please tell me the age of each person you have listed.
- 102 To which ethnic group or race does each of these individuals belong?
- 103 What is the gender of each person you have listed.

5b. [If "Single"], Have you ever been married?

## Empirical evaluation on other disease graphs



## Applying branching bandit formula to example

r is maximum instantaneous reward. In earlier example,  $\overline{r} = 1$ 

Ch(X) is set of children of node X

To define the Gittins index, let us first define two recursive functions  $\phi$  and  $\Phi$ , as per [KO03]. For any non-root node  $X \in \mathbf{X}$ , label  $b \in \Sigma$ , and value  $0 \le m \le \frac{\bar{r}}{1-\beta}$ ,

$$\phi_{X,b}(m) = \max \left\{ m, \sum_{v \in \Sigma} \mathcal{P}(X = v \mid \text{Pa}(X) = b) \cdot \left[ r(X, v) + \beta \cdot \Phi_{\text{Ch}(X), v}(m) \right] \right\}$$
(1)

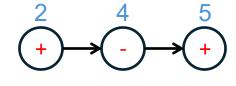
If X is the root, we define  $\phi_{X,\emptyset}(m) = \max \Big\{ m, \sum_{v \in \Sigma} \mathcal{P}(X = v) \cdot \big[ r(X,v) + \beta \cdot \Phi_{\mathrm{Ch}(X),v}(m) \big] \Big\}$ .

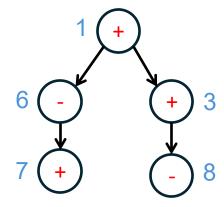
For any subset of nodes  $S \in X$ , label  $b \in \Sigma$ , and value  $0 \le m \le \frac{\bar{r}}{1-\beta}$ ,

parent's realizations don't affect X's value

The subscripts 
$$b$$
 don't matter because 
$$\Phi_{\mathbf{S},b}(m) = \begin{cases} \frac{\bar{r}}{1-\beta} - \int_{m}^{\frac{\bar{r}}{1-\beta}} \prod_{Y \in \mathbf{S}} \frac{\partial \phi_{Y,b}(k)}{\partial k} \ dk & \text{if } \mathbf{S} \neq \emptyset \\ m & \text{if } \mathbf{S} = \emptyset \end{cases}$$

$$g(X,b)=\min\left\{m\in\left[0,rac{ar{r}}{1-eta}
ight]:\phi_{X,b}(m)\geq m
ight\}$$
 The only non-zero term in summation is





The only non-zero when *v* is exactly the realized +/- label

## Maximizing non-decreasing submodular functions are well-studied in the literature

## Select subset S of elements such that f(S) is maximized

• f is a non-decreasing and submodular function

## Classic setting: selection S satisfies cardinality constraint, i.e., |S| ≤ b

- 1 1/e approximation via simple greedy algorithm [NWF78]
  - Until you run out of budget, pick the next item that maximizes marginal gain
- Cannot obtain better approximation ratio unless P = NP [Fei98]

#### Extension: selection S satisfies k matroid constraints

- 1 / (k+1) approximation achievable and tight for "local greedy" [FNW78]
  - · High-level idea: Run greedy for each matroid
- For single matroid (k = 1), 1 1/e approx. achievable via complicated rounding [CCPV11]
- Remark: cardinality constraint is a special case of partition matroid

## Lessons learnt and personal takeaways

#### 1. A useful problem formulation is a non-trivial contribution

- A good problem formulation is half the battle won
- Real-world are high-stakes yet often vaguely defined
  - "I want my process to be more efficient" → In what aspect?
  - "I want the allocation to be fair" → How to quantify?
- Problem formulation isn't about over-simplification, but about abstracting the key essence of the problem: "All models are wrong, but some are useful" – George Box [Box79]
- Careful modeling requires *close collaboration with domain experts* who share a mutual understanding of the problem and mutual trust, and appreciation of the work involved

## 2. Real-world settings often have structures to exploit

Principally designed methods can beat simple heuristics, even if assumptions are imperfect

## 3. Learning-augmented algorithms are a powerful and practical tool

Improve processes while respecting domain expertise in the age of AI and getting buy-in